A New Compact and Wide-band Band-stop Filter Using Rectangular SRR

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Abstract
This paper proposes a novel compact band-stop filter based on Rectangular SRR unit cell. The BSF structure consists of modified microstrip line connected to 50 Ω feed line on both sides and Rectangular-SRR which has been added and located in the center of the proposed design. The R-SRR dimensions are chosen and optimized in order to achieve a resonant frequency in the undesired band. This filter is designed, simulated and optimized using two electromagnetic solvers. The circuit performances have been investigated and found to have an excellent BSF characterized by high power rejection level in the stop-band, low insertion loss in the both pass-bands and compact size. The experimental results illustrate that the proposed BSF achieves a wide fractional bandwidth of 72 % at 2.2GHz.

Keywords: microstrip, filter, band-stop, split ring resonator, metamaterials

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1. Introduction
Suppression of unwanted range frequencies and avoidance of noise are an important issue in the microwave and wireless communication systems. This special role is performed by microstrip band-stop filters. They have been widely used in several and various wireless systems and circuits due to their ease fabrication, integration and compatibility with others planar devices. Recently, the demand for compact size, low cost and high electrical performances BSFs is extensively increased due to the development of microwave components and all area of wireless communication. These specifications are not available by conventional and classical techniques. However, to achieve these goals several methods were explored over the years. Among them, defected ground structure (DGS), microstrip line with etched spiral resonators and metamaterials [1-12].

Metamaterials are engineered materials, their dimensions are so smaller than the wavelength of the interacting signals. They take unusual electromagnetic wave propagation properties from their structures rather than their basic compounds. In the electromagnetic field, these artificial materials are characterized by two effective constitutive parameters known as effective permittivity and permeability. These parameters describe the response of metamaterial structures to magnetic and electric fields [13-17].

The main goal of this paper is to design a new small and compact microstrip band-stop filter with high electrical performances. For these reasons, the rectangular split ring resonator is used and implemented in the structure design. To achieve desirable return loss, good insertion loss, and small size from the proposed design, various parameters were tuned and optimized using two electromagnetic solvers.

2. Rectangular Split Ring Resonator
The split ring resonators were firstly introduced by Pendry and the experimental verification of left-handed behavior was firstly achieved by Smith which used the combination of magnetic and electric resonators represented respectively by SRRs and wire medium. The first one provides the required μ-negative property and the metallic rods provide the ε-negative property. Nowadays, several research works and diverse techniques have been realized to
achieve the resonators with negative permeability which have many useful advantages of microwave devices in term of size and electrical performances.

The SRR is basically constituted of two concentric enclosed Rings with splits in them at opposite sides. Due to the presence of the small space between the outer and inner rings, the SRR structure has a resonant wavelength larger than the diameters of these rings. This small distance and gap in the both rings produce high capacitive values that decreases the value of the resonance frequency which is given by Equation (1).

\[ f = \frac{1}{2\pi\sqrt{LC}} \]  

(1)

The effective medium theory is very useful to extract the material parameters from the normal scattering parameter data when analytical techniques are not easy to apply. The metamaterial characteristics of the chosen SRR unit cell are verified using Nicolson-Ross-Weir (NRW) approach. The NRW approach based on two composite terms \( V_1 \) and \( V_2 \) represent respectively the addition and subtraction of S-parameters given by Equation (2) and (3).

\[ V_1 = S_{21} + S_{11} \]  

(2)

\[ V_2 = S_{21} - S_{11} \]  

(3)

where the effective permeability and permittivity are related to parameters response by Equations (4) and (5).

\[ \mu_{eff} = \frac{2}{JK_0d} \frac{1-V_2}{1+V_2} \]  

(4)

\[ \varepsilon_{eff} = \frac{2}{JK_0d} \frac{1-V_1}{1+V_1} \]  

(5)

where \( K_0 \) presents a wave number equivalent to \( 2\pi/\lambda_0 \), \( d \) is the thickness of the substrate.

At first, the proposed rectangular split ring resonator is designed on an FR4 substrate and its dimensions are chosen after many series of optimization in order to achieve a resonant frequency around 2GHz. Its geometry is illustrated in Figure 1, where \( L = 11 \text{mm}, W = 9 \text{mm}, D = 1 \text{mm} \) and \( g = 0.5 \text{mm} \). Figures 2(a) and 2(b) show respectively the frequency response of the rectangular SRR and extracted real and imaginary of the permeability.

Figure 1. Geometry of the proposed R-SRR
3. Analysis and design of the proposed band-stop filter

A compact and miniaturized microstrip band-stop filter was built by using Rectangular SRR unit cell. Due to its relatively low cost, the proposed circuit is printed on Flame Resistant 4 epoxy substrate which is characterized by a relative permittivity of 4.4, a loss tangent of 0.025 and a thickness $h=1.6$ mm.

The geometrical configuration parameters of the proposed BSF based on rectangular Split Ring Resonator is shown in Figure 3. It consists of two 50 $\Omega$ transmission lines connected with modified U-shaped and the proposed resonator which is added and located exactly in the center of the structure, the circuit of the optimized BSF is very simple so that the manufacturing complexity can be reduced. It has a compact size of 17x20mm$^2$ excluding the feed lines. Where $L_1=12.5$mm, $W_1=13$mm, $L_2=3$mm and $S=1$mm.

![Figure 3. Geometry of the proposed band-stop filter](image)

To meet the requirement of the band-stop filter features in term of size and electrical performances of the rejected band and both passbands, several simulated results have been carried out and analyzed in order to choose the best one which satisfies the desired BSF filter specifications.

First of all, the proposed structure without metamaterial resonator has been simulated so as to understand the influence of the chosen rectangular SRR unit cell. It is plain to see from the Figure 4, that there is a normal transmission and no cut band is noticed in overall range frequencies extending from DC to 6GHz.
In order to achieve the BSF behavior, the rectangular split ring resonator has been implemented and all its parameters have been studied. In this investigation we just focused on the effect of two parameters. The first one is the R-SRR length which was varied from 10 mm to 11.5 mm in steps of 0.5 mm by keeping the all other parameters unchanged. Figure 5(a) and Figure 5(b) illustrate respectively the return loss and insertion loss against frequency for distinct values of the length $L_r$. As might be seen, it is possible to extend the bandwidth of the rejected band and moreover the central frequency of the BSF can be shifted from 2.7 GHz to 2.4 GHz by increasing the $L_r$. 

![Figure 5(a) Simulated return loss for different value of R-SRR length](image1)

![Figure 5(b) Simulated insertion loss for different value of R-SRR length](image2)
The second investigation was obtained by changing the value of the R-SRR width $W_r$ from 8mm to 9mm with all other parameters remains invariant. It is clearly observed from Figure 6, that as the $W_r$ is increasing the central frequency of the rejected band is decreasing. Furthermore, the second pass-band can be improved and its reflection-zero can be controlled and shifted by means of the R-SRR width.

![Figure 6. (a) Simulated return loss for different value of R-SRR width](image)

![Figure 6. (b) Simulated insertion loss for different value of R-SRR width](image)

The final scattering parameters of the proposed BSF are presented in Figure 7. As can be seen, the filter shows band-stop characteristic at the center frequency of 2.4 GHz and bandwidth of rejected band as 1.75 GHz [1.5GHz, 3.25GHz] with a deep rejection band of 40 dB. This filter is characterized by a stopband fractional bandwidth FBW of 70% that is given by Equation (6).

$$FBW = \frac{f_2 - f_1}{f_0} \times 100\%$$  \hspace{1cm} (6)
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4. Fabrication and Measurement

After numerous series of optimization by using two electromagnetic solvers CST Microwave and ADS Agilent. The obtained circuit has been fabricated on a 1.6 mm thick FR4 substrate by using LPKF machine. The fabricated BSF based on rectangular SRR prototype photograph is illustrated in Figure 9. It has a compact circuit size of 17x20 mm² without 50 Ω microstrip lines, the SMA connectors were soldered to the edge of the both BSF sides.

The measurements were achieved by an R&S Vector Network Analyzer HP 8719ES. The Simulated and measured S-parameters are compared in Figure 9. It can be clearly seen that there is an excellent agreement between them.

The return loss and insertion loss indicate that the fabricated BSF with FWB= 72% and a central frequency of 2.2GHz. It provides a power rejection level can reach more than 25 dB and good return and insertion loss have achieved in both passbands. The slight deviations between the simulated and measured results are mainly caused by dielectric losses or an error in the manufacturing or measuring process.
Figure 9. (a) Photograph of The Fabricated Band-Stop Filter density at the frequency 1GHz (b) Simulated and measured S-parameters of the BSF

The fabricated band-stop filter performances are compared with other published studies in Table 1, in term of overall size, rejected band, deep rejection and stopband fractional bandwidth FBW which is used to evaluate the rejected band of a BSF. As depicted in Table 1, we can obviously observe that this filter shows remarkable electrical performances, small size and wide stop-band characterized by a good attenuation level.

Table 1. The Performances comparison among published BSF filters and this work

<table>
<thead>
<tr>
<th>Parameters /Ref</th>
<th>Rejected band (GHz)</th>
<th>FBW</th>
<th>S21 deep (dB)</th>
<th>Size (mm²)</th>
</tr>
</thead>
<tbody>
<tr>
<td>[3]</td>
<td>[1.3-1.9]</td>
<td>37%</td>
<td>30</td>
<td>1000x</td>
</tr>
<tr>
<td>[5]</td>
<td>[2-3.2]</td>
<td>75%</td>
<td>30x</td>
<td>1100x</td>
</tr>
<tr>
<td>[9]</td>
<td>[0.975-1.025]</td>
<td>5%</td>
<td>35</td>
<td>6370x</td>
</tr>
<tr>
<td>[10]</td>
<td>[1.3-2.3]</td>
<td>55%</td>
<td>25x</td>
<td>1000x</td>
</tr>
<tr>
<td>This work</td>
<td>[1.4-3]</td>
<td>72%</td>
<td>25x</td>
<td>500</td>
</tr>
</tbody>
</table>

5. Conclusion

A novel compact microstrip band-stop filter based on rectangular-SRR unit cell has been proposed in this paper. The rejected band has been achieved by using metamaterial resonator which was added and implemented in the middle top layer of designed structure. It was developed and simulated using two different electromagnetic solvers and was fabricated and printed on an FR4 substrate. The proposed BSF has many desirable features such as small and compact size, wide stop-band and good electrical performances. This circuit with these characterizations will be a good choice to be implemented in modern communication systems.

Acknowledgement

We thank Mr. Mohamed Latrach Professor in ESEO, engineering institute in Angers, France, for allowing us to use all the equipment and solvers available in his laboratory.

References

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